



# Structural and Practical Identifiability Analysis of Models for Syncytia Growth

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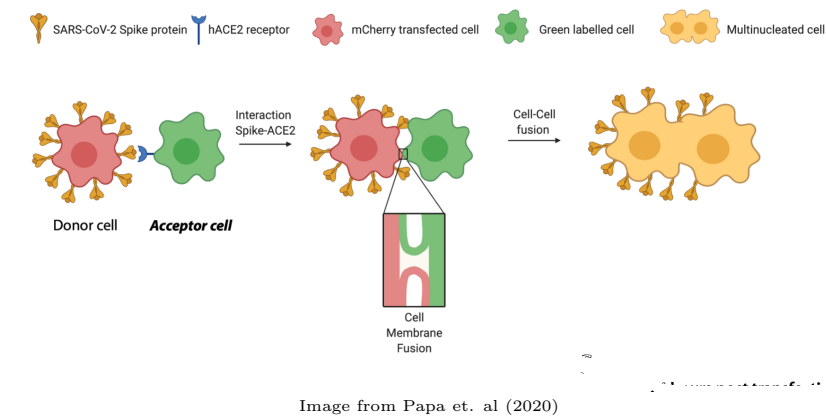
## Background

- Syncytia are multi-nucleated cells that can occur due to virus infections.
- To better understand viral dynamics it is important to understand how syncytia populations evolve during an infection.
- Syncytia can be cultured in vitro to obtain data about their growth over time.
- Ordinary Differential Equation (ODE) models can be used to model the growth of syncytia both in vivo and in vitro.
- Before actual experimentation it is essential to ensure we acquire the correct amount and type of data to parameterize the model.

## Structural and Practical Identifiability Analysis

- **Structural Identifiability** of an ODE model refers to the ability to estimate a model's parameters from its outputs. If a model is structurally identifiable, we can estimate parameter values from a given output measurement. Structural Identifiability Analysis refers to determining if a model is structurally identifiable, and it is a prerequisite before trying to fit a model to experiment data.
- **Practical Identifiability** of a model refers to the ability to determine the parameter values of a model under experimental conditions. Practical Identifiability analysis incorporates noise in output measurements and limited data sampling to replicate experimental conditions.

## Cell-Cell Fusion Assay



- One group of cells (donor cells) expresses the virus surface protein and is stained with one dye.
- A second group of cells (acceptor cells) expresses the cell surface receptor and is stained with a second dye.
- When the cells fuse, the syncytia will fluoresce with both dyes.
- Experiments typically measure the area covered by syncytia as a function of time.

## Model Overview

- We can write ODEs relating the donor cells (D), acceptor cells (A), and syncytia (S) that can predict the evolution of syncytia over time.
- We propose 3 models for syncytia growth to be analyzed.
- The models include the following parameters that need to be determined from the data.

Parameter	Name
$\gamma$	Syncytia Formation Rate
$N$	Max Population
$k$	Fusion Rate
$D_0$	Initial Number of Donors
$\delta$	Syncytia Death Rate

## Asymmetric & Symmetric Models

The asymmetric model is a simple model for syncytia fusion consisting of only acceptors, donors, and syncytia cells. The transition to syncytia is proportional to parameter  $\gamma$ .

$$\begin{aligned}\frac{dD}{dt} &= -\gamma DA \\ \frac{dA}{dt} &= -\gamma DA - \gamma SA \\ \frac{dS}{dt} &= 2\gamma DA + \gamma SA\end{aligned}$$

The symmetric model adds a term to account for the fusion of donor cells into existing syncytia.

$$\begin{aligned}\frac{dD}{dt} &= -\gamma DA - \gamma SD \\ \frac{dA}{dt} &= -\gamma DA - \gamma SA \\ \frac{dS}{dt} &= 2\gamma DA + \gamma SA + \gamma SD \\ N &= D + A + S\end{aligned}$$

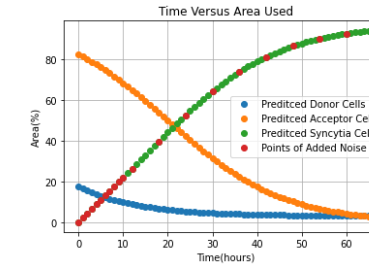
## Model With Death and Fusion

In this model, syncytia can die, and before syncytia can fuse there is a transitory fusing phase. The rate of fusion and death are represented by the parameters  $k$  and  $\delta$  respectively.

$$\begin{aligned}\frac{dD}{dt} &= -\gamma DA \\ \frac{dA}{dt} &= -\gamma DA - \gamma SA \\ \frac{dF_1}{dt} &= 2\gamma DA + \gamma SA - kF_1 \\ \frac{dF_2}{dt} &= kF_1 - kF_2 \\ \frac{dS}{dt} &= kF_2 - \delta S\end{aligned}$$

## Example Model Data

An example of the data that these models can simulate can be seen below.



## Identifiability of Models

We can analyze the identifiability of a system using Maple and a package called SIAN (Structural Identifiability Analyzer). We found that all models were identifiable for all relevant parameters when only Syncytia was measured.

### Monte Carlo Simulation

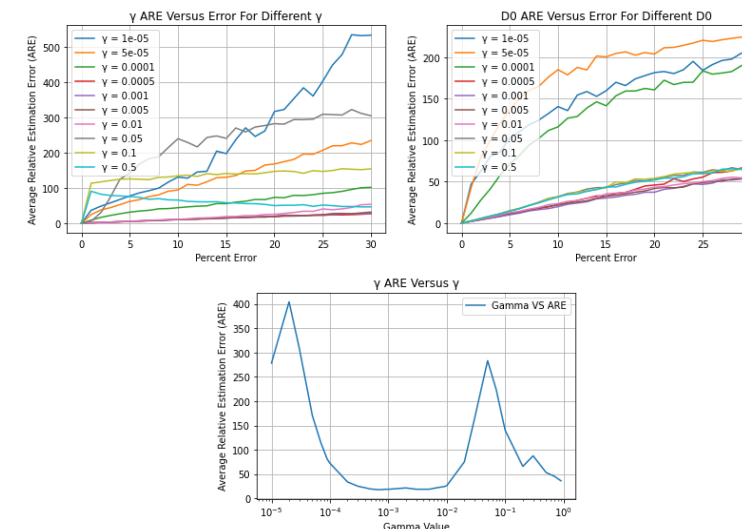
Monte Carlo simulations involve creating surrogate data with noise using set parameters and fitting our model to it. We can then estimate the parameter values from this surrogate data and compare them to actual parameter values. To do this we compute the average relative estimation error (ARE).  $\theta_0$  is the actual parameter value, and  $\theta_i$  is the estimated parameter value from our simulated data set.

$$ARE = 100\% \times \sum_{i=1}^N \frac{|\theta_0 - \theta_i|}{|\theta_0|}$$

## Monte Carlo Simulations

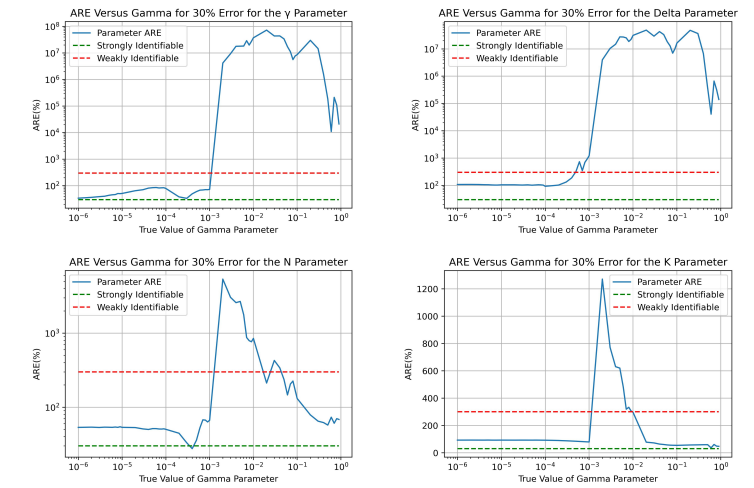
When doing Monte Carlo Simulations for practical identifiability 3 primary factors can affect parameter estimation.

- Sampling time and frequency
- Actual Parameter Value
- Measurement Noise

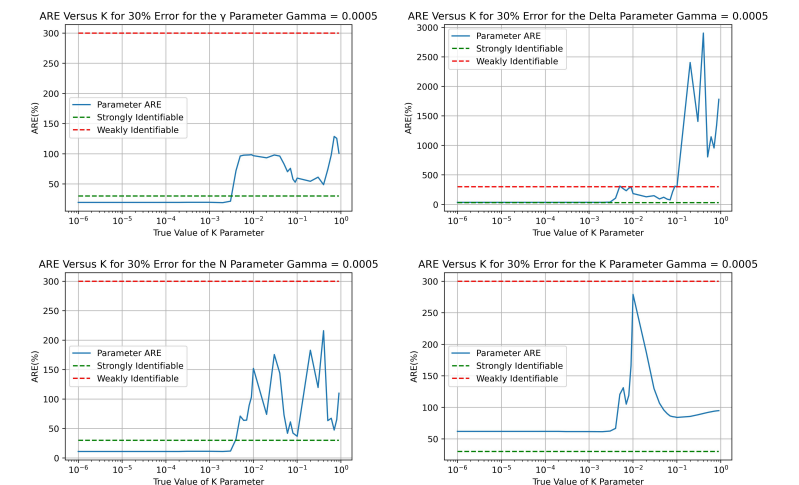


## Monte Carlo Simulations Continued

Below are the results of the Monte Carlo Simulations for the model with death and fusion showing estimation error for different parameters is affected by the value of the  $\gamma$  parameter.



Additionally, we can analyze how the estimation error is affected by changes in values of the  $k$  parameter.



## Conclusions

- Using SIAN for analysis, we were able to determine the structural identifiability of novel ODE models for syncytia growth.
- Practical identifiability analysis provides data on how parameter estimation is affected by experimental details and limitations.
- Knowledge of practical identifiability can inform experimental design so we may accurately parameterize our models.
- In these models, practical identifiability depended on sampling frequency, parameter value, and measurement error.
- Additional models can be considered for Syncytia growth.